

# Evaluating Off-Policy Evaluation: Sensitivity and Robustness

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## Take-Home Message

- In applications such as recommender systems, we often want to **evaluate the performance of a policy in an offline manner** (OPE), without any risky online interaction.
- When applying OPE to a real-world problem, **we need to identify a robust estimator that works without significant hyperparameter tuning.**
- Identifying a robust estimator is extremely difficult with a typical experimental procedure used in OPE research.
- We develop a novel evaluation protocol, *Interpretable Evaluation for Offline Evaluation*, which can **provide insights on the estimators' robustness.** (We also publicized a Python package, *pyIEOE*.)
- We **apply our procedure in a real-world e-commerce platform** and provide a suitable estimator choice for the platform.

## Off-Policy Evaluation

We consider a general contextual bandit setting.

- $x \in \mathcal{X}$  is a context vector (e.g., the user's demographic profile)
- $a \in \mathcal{A}$  is an action (e.g., an item recommended from a finite set of items)
- $r \in [0, r_{\max}]$  is a reward (e.g., click indicator on the recommended item)

Decision making systems (e.g., recommender systems) are often constructed by a policy  $\pi : \mathcal{X} \rightarrow \Delta(\mathcal{A})$ , which chooses an action for each given context to maximize the following policy value (i.e., expected reward).

$$V(\pi) := \mathbb{E}_{(x,a,r) \sim p(x)\pi(a|x)p(r|x,a)}[r], \quad (1)$$

where  $p(x)$  and  $p(r | x, a)$  are unknown provability distributions.

Here, we assume that we have a historical logged bandit data obtained by a *behavior* policy  $\pi_b$ :  $\mathcal{D} := \{(x_i, a_i, r_i)\}_{i=1}^n \sim \prod_{i=1}^n p(x)\pi_b(a | x)p(r | x, a)$ , where  $n$  is the data size.

*off-policy evaluation* (OPE) **aims to evaluate the performance of a counterfactual evaluation policy**  $\pi_e$  using only  $\mathcal{D}$  as follows.

$$\hat{V}(\pi_e; \mathcal{D}, \theta) \approx V(\pi_e), \quad (2)$$

where  $\hat{V}$  is an OPE estimator, and  $\theta$  is a set of estimator's (pre-defined) hyperparameters. Below, we show several examples of OPE estimators.

- **IPW** mitigates distribution shift between  $\pi_b$  and  $\pi_e$  using importance sampling techniques as  $\hat{V}_{IPW} := \mathbb{E}_n[\rho(x_i, a_i)r_i]$ , where  $\mathbb{E}_n[\cdot]$  is empirical average over  $\mathcal{D}$  and  $\rho(x_i, a_i) := \pi_e(x_i | a_i)/\pi_b(x_i, a_i)$  is the importance weight. This estimator is hyperparameter free but can suffer from large variance.

## Algorithm 1 Interpretable Evaluation for Offline Evaluation

**Input:** logged bandit feedback  $\mathcal{D}$ , an estimator to be evaluated  $\hat{V}$ , a candidate set of hyperparameters  $\Theta$ , a set of evaluation policies  $\Pi_e$ , a hyperparameter sampler  $\phi$  (default: uniform distribution), a set of random seeds  $\mathcal{S}$

**Output:** empirical CDF,  $\hat{F}_Z$ , of the squared error (SE)

- 1:  $\mathcal{Z} \leftarrow \emptyset$
- 2: **for**  $s \in \mathcal{S}$  **do**
- 3:    $\theta \leftarrow \phi(\Theta; s)$
- 4:    $\pi_e \leftarrow \text{Unif}(\Pi_e; s)$
- 5:    $\mathcal{D}^* \leftarrow \text{Bootstrap}(\mathcal{D}; s)$
- 6:    $z' \leftarrow \text{SE}(\hat{V}; \mathcal{D}^*, \pi_e, \theta)$
- 7:    $\mathcal{Z} \leftarrow \mathcal{Z} \cup \{z'\}$
- 8: **end for**
- 9: Estimate  $F_Z$  using  $\mathcal{Z}$  (by Eq. 1)

- **SNIPW** tries to address the variance of IPW by dividing  $\hat{V}_{IPW}$  by the sum of importance weights as  $\hat{V}_{SNIPW} := \mathbb{E}_n[\rho(x_i, a_i)r_i]/\mathbb{E}_n[\rho(x_i, a_i)]$ . This estimator is also hyperparameter free.
- **DR** also attempts to tackle the variance of IPW by leveraging baseline estimation  $\hat{q}$  and perform importance weighting only on its residual as  $\hat{V}_{DR} := \mathbb{E}_n[\mathbb{E}_{a \sim \pi_e(a|x)}[\hat{q}(x_i, a)] + \rho(x_i, a_i)(r_i - \hat{q}(x_i, a_i))]$ . To use DR, we have to set hyperparameters of  $\hat{q}$ .
- **Switch-DR** aims to further reduce variance of DR by avoiding importance weighting when  $\rho$  is large as  $\hat{V}_{\text{Switch-DR}} := \mathbb{E}_n[\mathbb{E}_{a \sim \pi_e(a|x)}[\hat{q}(x_i, a)] + \rho(x_i, a_i)\mathbb{I}\{\rho(x_i, a_i) \leq \tau\}(r_i - \hat{q}(x_i, a_i))]$ . This estimator have two hyperparameters,  $\hat{q}$  and  $\tau$ .

## Conventional Evaluation and Limitation

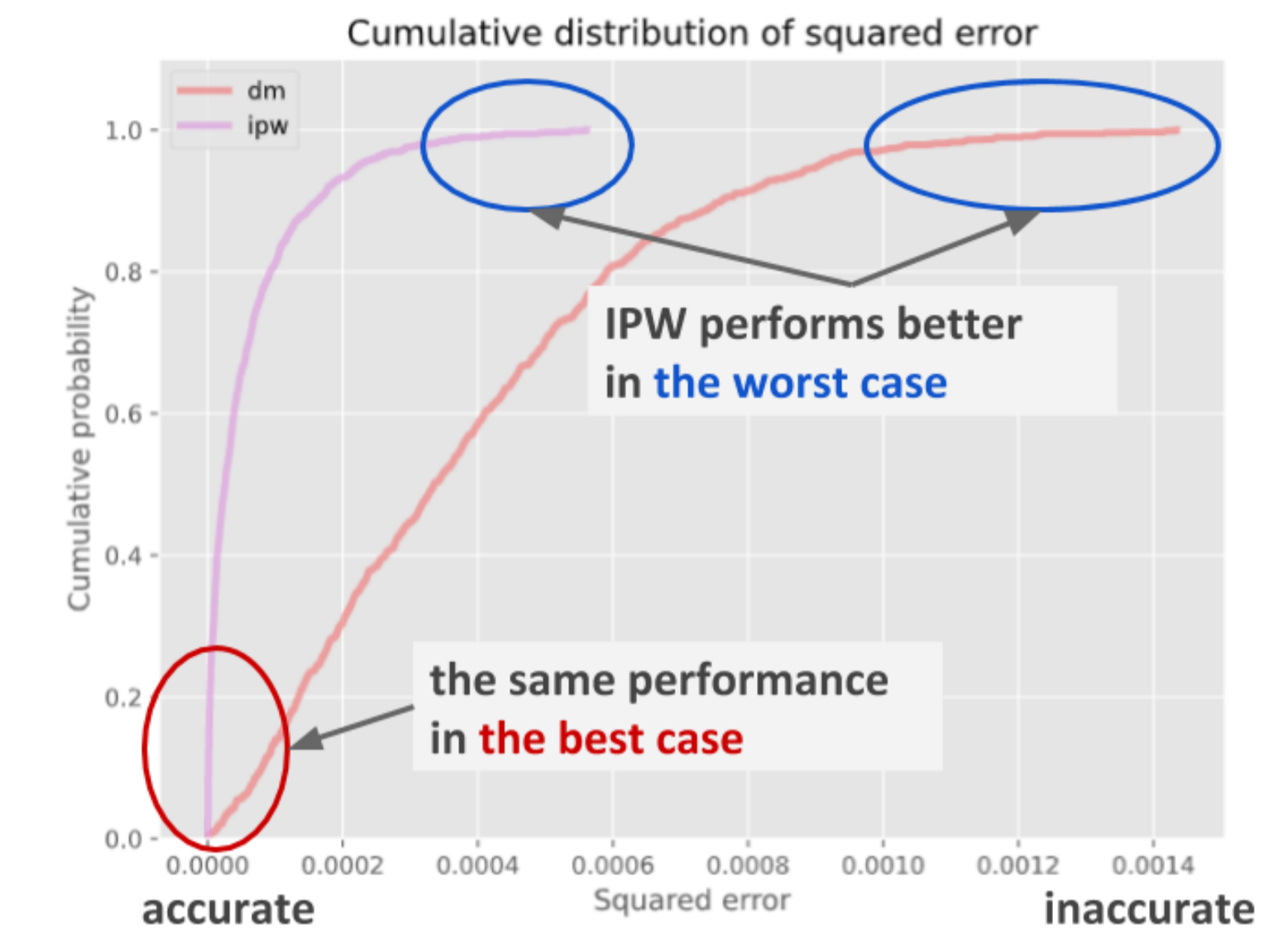
To evaluate and compare the performance of OPE estimators, we use the following *squared-error* (SE) as a performance measure for any given  $\pi_e, \mathcal{D}, \hat{V}, \theta$ .

$$\text{SE}(\hat{V}; \pi_e, \theta) := (V(\pi_e) - \hat{V}(\pi_e; \mathcal{D}, \theta))^2, \quad (3)$$

A typical evaluation procedure calculates **mean-squared-error (MSE) for a single given set of  $(\pi_e, \mathcal{D}, \theta)$**  to compare the performance of OPE estimators. We argue that **this typical procedure cannot evaluate the estimators' robustness to the configuration changes** of  $(\pi_e, \mathcal{D}, \theta)$ .

## Interpretable Evaluation for Offline Evaluation (IEOE)

To measure the estimators' robustness, we first calculate SE on a various set of configurations as shown in Algorithm 1. Moreover, we use



**cumulative distribution function (CDF) to conduct a more informative comparison** of the estimators' performance. CDF is a function defined as  $F_Z(z) := \mathbb{P}(Z \leq z)$ , which is the probability that the estimator achieves a performance better or equal to  $z$ . When we have  $\mathcal{Z} = \{z_1, \dots, z_m\}$  (which corresponds to SE), we can estimate CDF as follows.

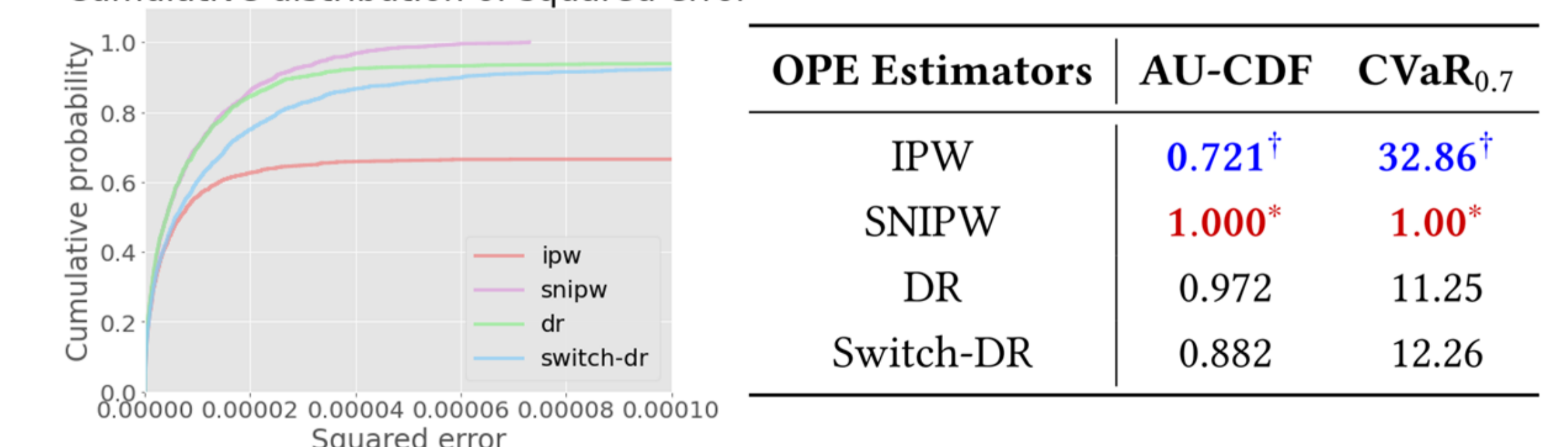
$$\hat{F}_Z(z) := \frac{1}{m} \sum_{i=1}^m \mathbb{I}\{z_i \leq z\}, \quad (4)$$

We can **visualize CDF for an interpretable comparison** as we show in the above figure. Using CDF, we also define evaluation metrics such as **area under the CDF curve**  $\text{AU-CDF}(z_{\max}) := \int_0^{z_{\max}} F_Z(z) dz$  and **conditional value-at-risk**  $\text{CVaR}_\alpha(Z) := \mathbb{E}[Z | Z \geq F_Z^{-1}(\alpha)]$ , which will be useful for identifying the robust OPE estimators.

## Real World Application

We applied the IEOE procedure to provide a suitable estimator choice for a real e-commerce platform. In the experiment, we found SNIPW clearly outperforms other estimators across various configurations on the platform data. **The platform is now using SNIPW after the comprehensive accuracy and stability verification with IEOE.**

Cumulative distribution of squared error



Note: Larger value of AU-CDF and lower value of CVaR indicate that the estimator is more accurate. We use  $z_{\max} = 5.0 \times 10^{-5}$  and  $\alpha = 0.7$ . The colors correspond to **best** and **worst**. The value is divided by that of the best estimator.

**Check out our camera-ready/arXiv paper for more detailed results! Also, feel free to ask any questions.**